


## Perspective

# The Use of VGPM to Estimate Oceanic Primary Production: A “Tango” Difficult to Dance

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One of the primary goals of launching an ocean color satellite is to obtain over the global ocean synoptic measurements of primary production (PP), a measure of phytoplankton photosynthesis. To reach this ultimate goal, in addition to precise measurements of radiance at the satellite altitude and robust data processing systems, a key requirement is to link primary production with satellite-derived products, where a model must be developed and applied. Although many models have been developed in the past decades, the vertically generalized production model (VGPM) developed by Behrenfeld and Falkowski, due to its simplicity and ease of use with satellite products, has been a de facto “standard” for the estimation of PP from ocean color measurements over the past 20+ years. Thus, it has significantly influenced the ocean color remote sensing and the biological oceanographic communities. In this article, we discuss the limitations of VGPM (and PP models based on chlorophyll concentration) in estimating primary production.

## 1. Summary of VGPM

Phytoplankton are ubiquitous in aquatic ecosystems and play a critical role in the food web and in carbon and energy cycles. The growth of phytoplankton is driven by photosynthesis, and this process can be measured from carbon fixation or primary production (PP). Thus, it is no surprise that “rational estimate of the growth of phytoplankton over long periods and large regions ... must be one of the central goals of biological oceanography” [1]. However, although there have been 10’s of thousands in situ measurements of PP in the global ocean in the past 6+ decades since Steemann Neilsen introduced the <sup>14</sup>C tracer technique [2], it is “infinite-simal” in view of the tremendous size of the ocean where phytoplankton vary greatly in space and time. It has been concluded decades ago [1, 3, 4] that a combination of both in situ measurements and satellite remote sensing is the only feasible means to obtain a rational estimate of PP of the global ocean for different time windows.

Satellite sensors do not provide a direct measurement of PP, but rather related properties that can be used to estimate PP, where a model must be applied. This is basically a pro-

cess to scale up discrete in situ data to broad-scale estimates guided or constrained by satellite measurements. Since such a model plays a key role in this process, many models have been developed over the past decades. In particular, because the concentration of chlorophyll-a (Chl, mg/m<sup>3</sup>) is routinely measured in oceanic surveys and that chlorophyll-a is the critical pigment for photosynthesis, the mainstream models for PP estimation are centered on Chl. These include simple empirical models simply converting Chl to PP (e.g., [5, 6]), which was basically an extension after the invention of fast measurement of Chl in the field through measurement of chlorophyll-a fluorescence [7]. The performance of such simple models is not always robust; more importantly, these models are purely empirical, which cannot provide a cause-effect understanding for the estimation of PP.

To represent the process of phytoplankton photosynthesis or carbon fixation mechanistically, a general and conceptual function for PP at depth  $z$  and time  $t$  can be expressed as [4, 8, 9]

$$PP(z, t, \lambda) = f(\text{Chl}(z); E(z, t, \lambda); \alpha^B(z), P_m^B(z)). \quad (1)$$

Here,  $\alpha^B$  is the initial slope of PP, while  $P_m^B$  is the asymptotic saturation rate at high light level, and both  $\alpha^B$  and  $P_m^B$  are values normalized to chlorophyll concentration or biomass (B). To get water-column PP over time and include all the contributions for wavelengths in the 400-700 nm domain, it simply means an integration of Eq. (1) over time, depth, and wavelength ( $\lambda$ ) [4]. Further, because conventionally Chl is taken as the key scaling parameter, and assuming that Chl of the global oceans can be well-estimated from satellite ocean color remote sensing, these models (after omitting wavelength dependence for brevity) can all be summarized in a conceptual form as [4, 10].

$$PP(z, t) = \text{Chl}(z) \times p(E(z, t); \alpha^B(z), P_m^B(z)), \quad (2)$$

with function  $p$  for the chlorophyll-normalized (or biomass-normalized) primary production. For this function  $p$ , Sathyendranath and Platt [4] stated that “Many equations have been proposed to represent the function  $p$ , with varying degrees of analytical explanations to support them. However, from a practical point of view, it has been shown by Platt et al. (1977) that most of these equations yield similar results for water column integrals of primary production, which would suggest that the choice of equation for  $p(I)$  is not a crucial one ...” Thus, it is not critical to spell out all the details of the various models regarding function  $p$  here. (The “ $I$ ” in Sathyendranath and Platt [4] is the intensity of photosynthetically available radiation (PAR), which is represented as  $E$  in this article.)

To calculate  $PP(z, t, \lambda)$  mechanistically, as articulated in Sathyendranath and Platt [4], it is required to know the following: (1) the vertical profile of Chl, (2) the value of PAR at surface ( $E_0$ , units as mol quanta  $m^{-2}$ ) and its propagation from surface to deeper depths ( $E(z)$ ), and (3) the estimates of the photosynthesis-light parameters (i.e.,  $\alpha^B$  and  $P_m^B$ ). Because ocean color remote sensing provides only averaged optical information of the upper layer of the water column, it is still a serious challenge even today to obtain accurate information of these properties over the water column, especially the photosynthesis-light parameters. Further, to obtain PP of large area over a long period of time, the complexity involved with Eqs. (1) and (2) poses a challenge for its broad application.

In view of the availability of both surface Chl and  $E_0$  of the global ocean from satellite ocean color remote sensing, after analyzing more than 10,000  $PP(z)$  profiles obtained from many regions of the global oceans, Behrenfeld and Falkowski [10] (represented as BF97 in the following) developed a simplified model for daily and water-column-integrated primary production. They bypassed the modeling of the details of  $p$  and focused instead on the  $P^B$  profiles of daily PP (note: symbols  $p$  and  $P^B$  represent the same property; since this article focuses on VGPM, we follow BF97 using  $P^B$  in the following for biomass-time-normalized PP), which is defined as

$$P^B(z) = \frac{PP(z, \text{daily})}{\text{Chl}(z) \times D_{\text{irr}}}. \quad (3)$$

Here,  $D_{\text{irr}}$  is the day length and measured in hours; thus, the units for  $P^B$  are  $\text{mg C (mg Chl)}^{-1} \text{h}^{-1}$ . Figure 1 shows examples of vertical profiles of daily  $PP(z)$  and  $P^B(z)$ . Subsequently, the focus of BF97 was on daily primary production, especially  $P^B$ , the “daily averaged” chlorophyll-normalized primary production, rather than the conceptual instantaneous property in Eq. (1).

For  $P^B(z)$ , BF97 further found that its profiles follow a similar pattern and used a relative vertical distribution of  $P^B$  (here represented as  $P_{\text{rel}}^B$  instead of  $P_{\zeta}^B$  in the original paper, as  $P_{\zeta}^B$  and  $P^B(\zeta)$  could be confused with each other), which is expressed as [10]

$$P_{\text{rel}}^B(\zeta) = \left[ 1 - \exp\left(-\frac{E(\zeta)}{E_{\text{max}}}\right) \right] \exp(-\beta_d \times E(\zeta)). \quad (4)$$

Here,  $\zeta$  is an optical depth, which is the product of  $K$  and  $z$ , with  $K$  (in  $m^{-1}$ ) for the attenuation coefficient of PAR and calculated from the euphotic zone depth ( $Z_{\text{eu}}$ , in meters)

$$K = \frac{-\ln(0.01)}{Z_{\text{eu}}}, \quad (5)$$

and  $\beta_d$  is the photoinhibition parameter. Further, BF97 obtained daily water-column integrated primary production ( $PP_{\text{eu-day}}$ ) as (note that the “-” sign in front of  $\beta_d$  in their original Eq. (8) was missing)

$$PP_{\text{eu-day}} = \frac{P_{\text{opt}}^B \times D_{\text{irr}}}{\left[ 1 - \exp\left(-E_{\text{opt}}/E_{\text{max}}\right) \right] \exp(-\beta_d \times E_{\text{opt}})} \cdot \int_0^{Z_{\text{eu}}} \left[ 1 - \exp\left(-\frac{E(z)}{E_{\text{max}}}\right) \right] \exp(-\beta_d \times E(z)) \times \text{Chl}(z) \times dz. \quad (6)$$

Solar radiation ( $E(z)$ ) at depth is (the expression in the original paper missed a “-” sign)

$$E(z) = E_0 \exp(-K \times z), \quad (7)$$

and  $E_{\text{opt}}$  is the solar radiation corresponding to the maximum  $P^B$  (represented as  $P_{\text{opt}}^B$ ), which can be calculated from

$$E_{\text{opt}} = E_0 \exp(-\zeta_{\text{opt}}). \quad (8)$$

$\beta_d$  and  $E_{\text{max}}$  are properties associated with photosynthesis [10]. Basically, Eq. (6) is the depth-resolved form of VGPM.

After empirically relating  $E_{\text{max}}$ ,  $\zeta_{\text{opt}}$ , and  $\beta_d$  with  $E_0$  [10], and considering  $\text{Chl}(z)$  can be moved out of the integration in Eq. (6) without much impact on  $PP_{\text{eu-day}}$ , BF97 finally

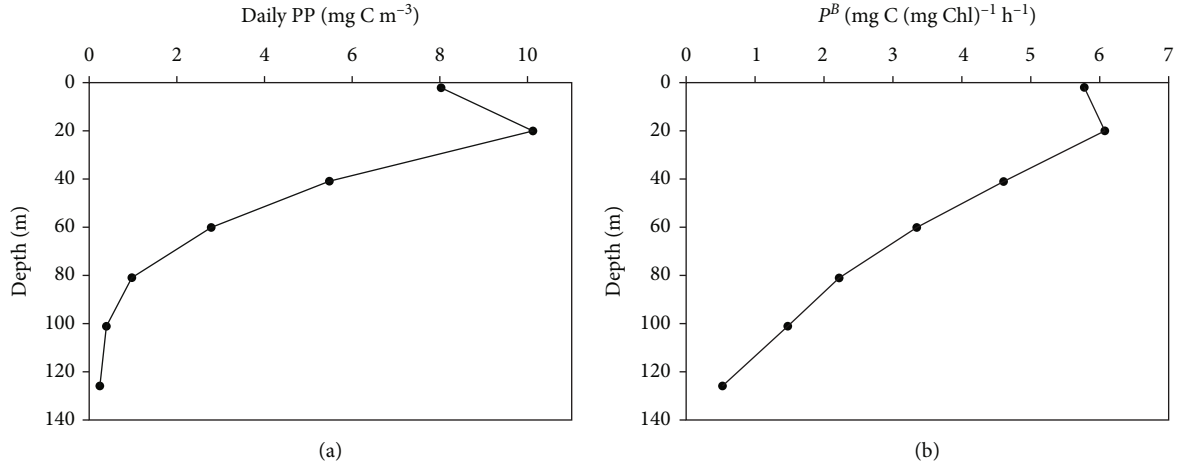


FIGURE 1: Examples (data from JFM) of daily PP profile (a) and the Chl-normalized, hourly,  $P^B(z)$  profile (b). The reduction of PP near surface is due to photoinhibition of photosynthesis that is omitted in Eq. (1) for simplicity, but it can be easily incorporated.

obtained the widely used VGPM for daily depth-integrated primary production as (Eq. (10) of BF97)

$$PP_{\text{eu-day}} = 0.66125 \times P_{\text{opt}}^B \times \frac{E_0}{E_0 + 4.1} \times Z_{\text{eu}} \times \text{Chl}_{\text{opt}} \times D_{\text{irr}}. \quad (9)$$

Note that the constant 4.1 has units as mol quanta m<sup>-2</sup> for a day. The maximum biomass-normalized photosynthesis parameter ( $P_{\text{opt}}^B$ ) was empirically parameterized from field data as a seventh-order polynomial function of temperature ( $T$ )

$$P_{\text{opt}}^B = \sum_{i=0}^7 v_i \times T^i. \quad (10)$$

Since  $E_0$  and Chl (which can be approximated as  $\text{Chl}_{\text{opt}}$  [10]) are standard products from ocean color satellites,  $T$  is available from satellites,  $Z_{\text{eu}}$  can be estimated from Chl [11], and  $D_{\text{irr}}$  can be easily calculated given date and location information, Eq. (9) becomes a very powerful and widely used tool to estimate daily water-column integrated PP of the global ocean.

This model for  $PP_{\text{eu-day}}$  is more complex than empirical models simply based on Chl, such as that proposed a decade earlier by Eppley et al. [12], which is

$$\log(PP_{\text{eu-day}}) = 3 + 0.5 \log(\text{Chl}), \quad (11)$$

where the Eppley model has no relationship of  $PP_{\text{eu-day}}$  to solar radiation. Figure 2 presents ratios of  $PP_{\text{eu-day}}/\text{Chl}$  obtained from Eq. (9) for a range of Chl and common values of  $E_0$  and  $T$ , which suggests that, for the same Chl,  $PP_{\text{eu-day}}$  estimated from VGPM could be 2-3 times higher than that obtained by the Eppley model (its ratios of  $PP_{\text{eu-day}}/\text{Chl}$  for the same Chl are also included in Figure 2).

## 2. A Few Caveats

The processes to reach Eq. (9) are not straightforward, and some terms are not clearly described or represented by symbols and could cause confusion. For instance,  $P_{\text{rel}}^B$  (originally as  $P_{\zeta}^B$ ), a “dimensionless” quantity, is termed as “relative vertical distribution,” but it was not clearly defined as “relative” to which property. Based on Figure 3(a) of BF97, it suggests that  $P_{\text{rel}}^B$  is defined as

$$P_{\text{rel}}^B(z) = \frac{P^B(z)}{P^B(\zeta_{\text{opt}})}. \quad (12)$$

By this definition,  $P_{\text{rel}}^B$  is in a range of 0–1 for its vertical profile, matching the patterns showing in Figure 3(a) of BF97. However, this  $P_{\text{rel}}^B$  is not consistent with Eq. (4), as the maximum value calculated from Eq. (4) for normal  $\beta_d$  and  $E_{\text{max}}$  will be less than 1. This difference suggests that although Eq. (4) represents a “relative vertical distribution,” it is not necessarily that of Eq. (12). As such, in order to compensate for the maximum value of Eq. (4) is less than 1, the following term

$$\left[ 1 - \exp\left(-\frac{E_{\text{opt}}}{E_{\text{max}}}\right) \right] \exp(-\beta_d \times E_{\text{opt}}) \quad (13)$$

is included in Eq. (6) as a denominator. Note that if  $P_{\text{rel}}^B$  is defined following Eq. (12) and modeled matching that showing in Figure 3(a) of BF97, there is no need to have such a denominator in Eq. (6).

Further, in the process to reach the final form for  $PP_{\text{eu}}$  (Eq. (9)), BF97 obtained the following integration (which is Eq. (9) of BF97)

$$\int_z P_{\text{rel}}^B(\zeta) = \frac{E_0}{E_0 + 4.1}. \quad (14)$$

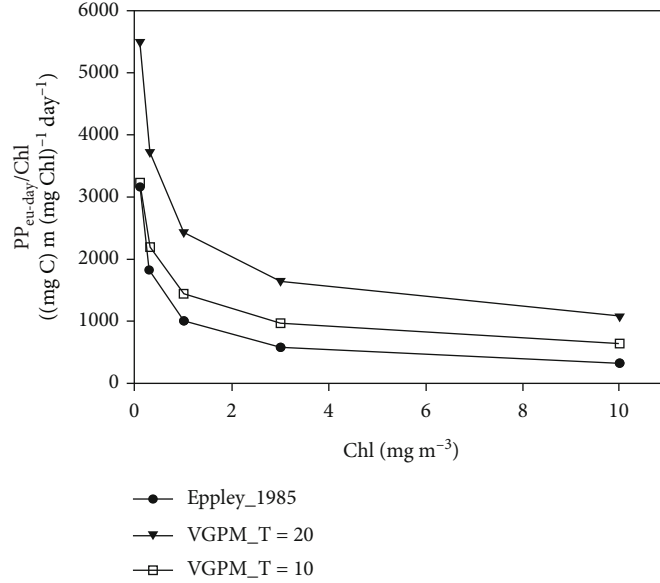


FIGURE 2: A comparison of  $PP_{eu-day}/Chl$  for  $Chl$  in a range of  $0.1-10 \text{ mg m}^{-3}$  calculated from VGPM and from the Eppley model. The temperatures used are included in the figure, while  $E_0$  is kept as  $40 \text{ mol quanta m}^{-2}$  and  $D_{irr}$  as 12 hours.

For a function as Eq. (4), there is no analytical solution for its integration over depth. Further, no matter if  $P_{rel}^B$  are the profiles shown in Figure 3(a) of BF97 or those represented by Eq. (4), the integration over depth in the left side of Eq. (14) will be greater than 1.0, while the right side of Eq. (14) will be always less than 1.0. This mismatch suggests that there must be a scaling somewhere in the integration in order to reach Eq. (14).

Since Eq. (14) could not be derived analytically, Eq. (9) was obtained through numerical simulations (Dr. Michael Behrenfeld, personal communication) and consequently, Eq. (9) is not exactly equal to Eq. (6). For  $E_0$  in a range of  $5-50 \text{ mol quanta m}^{-2}$  and  $Z_{eu}$  in a range of  $20-200 \text{ m}$ , the ratio of Eq. (9) to Eq. (6) is in a range of  $0.75-1.07$ , with higher deviation from 1 at low  $E_0$ . Compared to the large uncertainties in field measurement of primary production, this deviation in the numerical reduction of Eq. (6) to Eq. (9) is insignificant. This also indicates that the constant “0.66125” in Eq. (9) can be rounded to “0.7” or “0.66” without any significant impact on the performance of VGPM.

### 3. The “Tangling” of VGPM or Chl-Based PP Model

Tango, involving exciting movements, is a popular dance that originated in Argentina and is a pleasure to watch. VGPM, due to its simplicity and reasonable performance shown in BF97, is also very exciting for the biological oceanographic community. Tango requires two partners to cooperate nicely and precisely. For VGPM, since  $E_0$  and  $D_{irr}$  can be well estimated, and  $Z_{eu}$  can be estimated from  $Chl$ , it also requires two key “partners” to cooperate nicely. The two are  $Chl$  and  $P_{opt}^B$ , but the “tango,” a tangling of optics, biology and physiological properties in remote sens-

ing models, makes the “dance” not the level of a great show yet. Here are the reasons.

- (1) Presently, the  $Chl$  product of the global ocean from satellite ocean color measurements is generated with empirical algorithms, either band ratio [13] or band difference [14] (collectively termed as color index, CI) of the remote sensing reflectance ( $R_{rs}$ ). This CI, at least for oceanic waters, as illustrated in the literature [14, 15], represents the total absorption coefficient ( $a$ ) at the blue wavelength (normally around  $443 \text{ nm}$ ), where  $a(443)$  can be expressed as

$$a(443) = a_w(443) + a_{ph}^*(443) \times Chl + a_{dg}(443). \quad (15)$$

Here,  $a_w(443)$  is the absorption coefficient of pure (sea)water [16, 17], which varies slightly with temperature [18, 19],  $a_{ph}^*(443)$  is the chlorophyll-specific absorption coefficient, and  $a_{dg}$  is the absorption coefficient of detritus-gelbstoff. Thus, in addition to  $Chl$ , there are two “extra” variables governing the variation of  $a(443)$ :  $a_{ph}^*(443)$  and  $a_{dg}(443)$ . Even considering  $a_{dg}(443)$  to covary with  $Chl$ , the variation of  $a_{ph}^*(443)$  needs to be taken into account before we can accurately estimate  $Chl$  based on CI. An unpleasant truth is that  $a_{ph}^*(443)$  of the global ocean varies widely for the same  $Chl$  value [20], and there is still a big knowledge gap on an appropriate estimation of  $a_{ph}^*(443)$  from remote sensing. Without an understanding of the spatial-temporal variation of  $a_{ph}^*(443)$ , in the estimation of  $Chl$  from ocean color measurements we will be stalled at the current level [21].

- (2)  $P_{opt}^B$ , the “maximum  $C$  fixation rate within a water column”, is far from a constant (with its variation more than a factor of 2) for the same temperature (see Figure 7 in BF97) and varies in a complex manner. Following the same principle but taking a different mathematical form from Eq. (1), instantaneous PP can be expressed as [22–24]

$$PP(z, t, \lambda) = 12\text{Chl}(z, t) \times a_{ph}^*(z, t, \lambda) \times E(z, t, \lambda) \times \phi(z, t, \lambda). \quad (16)$$

Here,  $\phi$  is the photosynthetic quantum yield, and the constant 12 converts mol carbon to gram carbon. Thus, after integration over time and wavelength, Eq. (16) indicates that  $P_{opt}^B$  is

$$P_{opt}^B = \frac{PP(z)}{\text{Chl}(z) \times D_{irr}} \Big|_{\max} \propto a_{ph}^*(z) \times E(z) \times \phi(z) \Big|_{\max}. \quad (17)$$

This expression suggests that the value of  $P_{opt}^B$  depends on three properties: solar radiation ( $E$ ), photophysiology ( $\phi$ ), and  $a_{ph}^*$  at the depth (opt) where  $P^B$  is the maximum. This multivariate dependence of  $P_{opt}^B$  may explain why there are large variations of  $P_{opt}^B$  obtained from in situ measurements [10]. Consequently, it is difficult, if not impossible, to accurately estimate  $P_{opt}^B$  using temperature alone (Eq. (10)). As highlighted in Behrenfeld and Falkowski [10], “the accuracy of productivity algorithms in estimating  $PP_{eu}$  is dependent primarily upon the ability to accurately represent variability in  $P_{opt}^B$ .” However, since  $a_{ph}^*$ , a bio-optical property that varies widely, is a variable of  $P_{opt}^B$  (see Eq. (17)), an accurate estimation of  $P_{opt}^B$  remains challenging. This might be the main reason that Behrenfeld et al. [25] later concluded “... a clear path for globally modeling or remotely observing variability in chlorophyll-specific photosynthesis has even to this day never been identified.”

#### 4. Schemes to “Detangling” Optics and Biology for PP Estimation

From the above discussions, the biggest uncertainties in the remote sensing of PP via VGPM or similar Chl-based models is the “tangling” of optical and biological properties that is hooked explicitly or implicitly by  $a_{ph}^*$ ; thus, a detangling, i.e., a tango to allowing space for the two partners, is certainly plausible. Detangling can be achieved by excluding the involvement of  $a_{ph}^*$ . There have been two schemes proposed in the past decades for this. One is centered on the absorption coefficient of phytoplankton ( $a_{ph}$ ) [26] or the absorption-based approach (AbPM). Another, the “carbon-based approach” (CbPM) [25, 27] is centered on the backscattering coefficients of phytoplankton.

The AbPM scheme is a rearrangement of Eq. (16):

$$PP(z, t, \lambda) = 12 a_{ph}(z, t, \lambda) \times E(z, t, \lambda) \times \phi(z, t, \lambda), \quad (18)$$

as by definition  $a_{ph}$  is the product of Chl and  $a_{ph}^*$ . In this equation,  $a_{ph}$  is an optical property while  $\phi$  is a biological (or photophysiological) property. They are two different and independent properties that are not tangled or hooked by  $a_{ph}^*$ . While the value and variation of  $\phi$  have to be determined from in situ measurements,  $a_{ph}$  can be directly and analytically inverted from  $R_{rs}$  [28]. It is  $a_{ph}$  and  $\phi$  ( $E$  is a minor player as  $\phi$  also varies with  $E$ ) working together, a “tango”, to complete the estimation of PP from ocean color remote sensing, where significantly better estimates have been demonstrated [26, 29–31]. This might be the “tango” we should practice for the remote sensing of oceanic PP.

The CbPM scheme focuses on the phytoplankton biomass ( $C_{ph}$ ) with  $C_{ph}$  estimated from remotely sensed particle backscattering coefficient ( $b_{bp}$ ). Although an empirical relationship is required to convert  $b_{bp}$  to  $C_{ph}$ , where nonnegligible uncertainties exist, it also avoided the involvement of  $a_{ph}^*$  and showed promising results in explaining the decadal variations of global PP [25].

Nevertheless, by no means do we suggest that the above schemes have resolved all the issues and challenges associated with the remote sensing of PP, especially the vertical variations associated with biological and physiological properties [32–34]. Rather, it only indicates that it is not a requirement to include Chl (and then the involvement of  $a_{ph}^*$ ) in the algorithms or models. If Chl is included, the optical and biological properties will be tangled for the estimation of oceanic PP from ocean color remote sensing.

#### 5. Concluding Remarks

Although remote sensing of global PP based on ocean color measurements has been carried out for more than four decades, we are still far from the goal of achieving an accurate estimation of the spatial and temporal distributions of PP of the global oceans. While the VGPM developed by Behrenfeld and Falkowski [10] significantly advanced the application of satellite data for PP estimation and contributed to the overall estimates of global annual PP, the implicit embedding of  $a_{ph}^*$  in the determination of both Chl and  $P_{opt}^B$ , the two key players of VGPM and many other Chl-based models, makes the estimated PP for a region and at a specific time to have large uncertainties. To achieve more reliable PP estimates at regional and temporal scales, and to improve further the remote sensing of optical properties (especially  $a_{ph}$  and the backscattering coefficient of phytoplankton) from ocean color data and to obtain its vertical information, it is critical to have a better understanding and handling of the quantum yield of phytoplankton photosynthesis, where knowledge of phytoplankton functional types is important.

## Conflicts of Interest

The authors declare that they have no known conflict of interest or personal relationships that could have appeared to influence the work reported in this paper.

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